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A discrete dynamical system consists of a set S and a self-map $\phi : S \rightarrow S$, and one is then interested in classifying the points of S according to their behavior under iteration of the map ϕ . This subject has a long and storied history when S is an analytic space, for example \mathbb{R} , \mathbb{C} , or \mathbb{CP}^1 , and there are many deep and beautiful results of a geometric and analytic nature. During the past 25+ years people have developed an arithmetic theory of discrete dynamics, in which S is an arithmetic set such as \mathbb{Z} , \mathbb{Q} , or $\mathbb{P}^1(\mathbb{Q})$, and the map ϕ is a polynomial or rational function. In this setting one studies arithmetic properties of orbits under iteration of ϕ . In this talk I will give a survey of this new field of arithmetic dynamics, including some of its history, some known results, and some of the conjectures that motivate current research. (Received August 07, 2011)