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**Holly E Attenborough\*** (heattenb@indiana.edu), Bloomington, IN 47401. *A Decomposition for Idempotents of the Brauer Monoid.*

Let  $G = \text{Gal}(K/F)$  for a Galois field extension  $K/F$ . The Brauer Monoid,  $M^2(G, K)$  is defined by adapting the cocycle construction of the Relative Brauer Group,  $Br(K/F) = H^2(G, K^*)$ . We adapt the cocycles by allowing the image to be all of  $K$ , these cocycles,  $f : G \times G \rightarrow K$ , are called **weak** 2-cocycles. Let  $e$  an idempotent weak 2-cocycle, define the group  $M_e^2(G, K)$  to be  $\{[f] \in M^2(G, K) | ef = f\}$ . For a specific ring  $R_e$  associated with an idempotent  $e$ , we have a complex on  $R_e$ -modules,  $M^e$ , that gives us that  $M_e^2(G, K) \cong H^2(\text{Hom}_{R_e}(M^e, K^*))$ . The idempotents  $e$  are in one-to-one correspondence with lower subtractive partial orders on the group  $G$ ,  $e \mapsto \leq_e$ . For  $S$  and  $T$  lower subtractive subsets of  $G$ , such that  $S \cup T = (G, \leq_e)$ , there exists a split short exact sequence on the complexes:

$$0 \rightarrow \mathbf{M}^{S \cap T} \rightarrow \mathbf{M}^S \oplus \mathbf{M}^T \rightarrow \mathbf{M}^e \rightarrow 0.$$

This gives us a long exact sequence on cohomology, which can aid with the computation of  $H^2(\text{Hom}_{R_e}(M^e, K^*)) \cong M_e^2(G, K)$ . (Received September 17, 2012)