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**Nancy Eaton, Adam Gilbert** and **A. M. Heissan\*** (mia@math.uri.edu). *A coil  $G$  on  $n$  vertices is four-colorable.* Preliminary report.

Let  $G$  be a planar, inner-triangulated graph on  $n$  vertices whose depth-first search tree (DFS) is the path  $(v_1, v_2, \dots, v_n)$ . We call such a graph a *coil*. We define the *coil edges* to be the edges of the form  $(v_i, v_{i+1})$ . All other edges of  $G$  are *crossing edges*. The *up-neighborhood* of  $v_i$  is the non-empty set of vertices with indices all less than  $i - 1$ . If  $m$  is the number of crossing edges and  $\beta$  is the number of up-neighborhoods in  $G$ , we show that  $G$  is four-colorable with at least  $4 \cdot 3^{n-1} \left(\frac{2}{3}\right)^m \left(\frac{3}{4}\right)^{\beta-1}$  distinct colorings. (Received September 24, 2012)