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Let  $H$  and  $G$  be graphs such that  $G$  is a subgraph of  $H$ . A  $G$ -decomposition of  $H$  is a set  $\Delta = \{G_1, G_2, \dots, G_t\}$  of pairwise edge-disjoint subgraphs of  $H$  each of which is isomorphic to  $G$  and such that each edge of  $H$  occurs in exactly one  $G_i$ . Graham and Häggkvist have conjectured that every tree with  $n$  edges decomposes every  $2n$ -regular graph. This conjecture has been confirmed for a small number of cases. If  $T$  is a tree with  $n$  edges and  $G$  is  $n$ -regular, then  $T$  may or may not decompose  $G$ . For a simple graph  $G$ , we let  ${}^2G$  denote the multigraph obtained by replacing each edge of  $G$  with two parallel edges. El-Zanati conjectures that if a  $T$  is a tree with  $n$  edges and  $G$  is an  $n$ -regular simple graph, then there exists a  $T$ -decomposition of  ${}^2G$ . We show that this conjecture holds true when  $T$  is a bistar and  $G$  is triangle free. (Received September 25, 2012)