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**Neil Hindman** and **Dev Phulara\*** (phulara@comcast.net). *Some new additive and multiplicative Ramsey numbers.*

For  $a, r \in \mathbb{N}$ , the set of positive integers, define  $FSP_2(a, r)$  (respectively  $SP_2(a, r)$ ) to be the first  $n \in \mathbb{N}$ , if such exists, such that whenever  $\{1, 2, \dots, n\}$  is  $r$ -colored, there exist  $x$  and  $y$  with  $a \leq x < y$  such that  $\{x, y, x+y, xy\}$  is monochromatic (respectively  $\{x+y, xy\}$  is monochromatic). If no such  $n$  exists, the number is defined to be infinite. It is an old result of R. Graham that  $SP_2(a, 2)$  is finite for all  $a$ . With that exception, the only cases (with  $r > 1$ ) for which  $FSP_2(a, r)$  or  $SP_2(a, r)$  are known to be finite are those for which explicit values have been computed. We provide exact values of  $FSP_2(a, 2)$  for  $a \leq 5$  (of which  $FSP_2(1, 2)$  and  $FSP_2(2, 2)$  were previously known). We provide exact values of  $SP_2(a, 3)$  for  $a \leq 8$  and exact values of  $SP_2(a, 2)$  for  $a \leq 60$ . We also compute upper and lower bounds for  $SP_2(a, 2)$ . (Received September 07, 2012)