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**Barry R Smith\*** (barsmith@lvc.edu). *Divisibility of the equivariant  $L$ -function value at zero for degree  $2p$  extensions.* Preliminary report.

The equivariant  $L$  function value at zero of an Abelian extension of number fields  $K/k$  with Galois group  $G$  is an element of the rational group ring  $\mathbb{Q}[G]$ . Multiplying it by the number of roots of unity in  $K$  yields an element of the integral group ring  $\mathbb{Z}[G]$ , the “integralized  $L$ -value”. When  $p$  is an odd prime and  $K/k$  has degree  $2p$ , we show that the  $p$ -divisibility of the integralized  $L$ -value is usually determined in a simple way by the arithmetic of the quadratic extension of  $k$  contained in  $K$ . We also identify an extremely exceptional class of extensions  $K/k$  for which the situation is more complex; we conjecture that for such extensions, the  $p$ -divisibility of the integralized  $L$ -value is equivalent to a refinement of the Brumer-Stark conjecture for the quadratic sub-extension of  $K/k$  whose top field is  $K$ . We prove this conjecture under the assumption that the Brumer-Stark conjecture holds for  $K/k$ . (Received September 25, 2012)