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C. Sung*, 5201 University Boulevard, Laredo, TX 78041. *Some Recent Results on Odd Perfect Numbers*. Preliminary report.

A perfect number is a natural number N such that the sum of its positive divisors (including N) of N equals $2N$, denoted by $\sigma(N) = 2N$. From the work of Euclid and Euler, it is known that an even natural number N is perfect if and only if there is a natural number p such that $(2^p - 1)$ is a prime and $N = (2^p - 1)2^{(p-1)}$. Today, there are about 47 known even perfect numbers. Euler proved that for an odd perfect number N , there is a prime $p \equiv 1 \pmod{4}$ such that $N = (p^m)(q^2)$ with $m \equiv 1 \pmod{4}$ and $\gcd(p, q) = 1$. However, it is an unsolved problem in number theory whether there are any odd perfect numbers. In 1991, Brenti, Cohen, and de Riele proved that odd perfect numbers are greater than 10^{300} . In 2012, Ochem and Rao modified their method to show that odd perfect numbers are greater than 10^{1500} . Some recent results on odd perfect numbers will be discussed in this presentation. (Received September 26, 2012)