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William E Gryc* (wgryc@muhlenberg.edu), Department of Mathematics & Computer Science, Muhlenberg College, 2400 Chew St, Allentown, PA 18104, and **Todd Kemp**. *Sharpness Results for Duality in Segal-Bargmann Spaces*. Preliminary report.

For $\alpha > 0$ let γ_α denote the standard Gaussian probability measure on \mathbb{C}^n with variance $(2\alpha)^{-n}$. Let $L_{hol}^p(\gamma_{\alpha p/2})$ denote the holomorphic functions that are contained in $L^p(\gamma_{\alpha p/2})$. Janson, Peetre, and Rochberg showed that $L_{hol}^p(\gamma_{\alpha p/2})$ and $L_{hol}^{p'}(\gamma_{\alpha p'/2})$ are dual to each other under the L^2 -pairing $(\cdot, \cdot)_\alpha$ of $L_{hol}^2(\gamma_\alpha)$. In previous work the authors found an inequality of the equivalence of the norms. Specifically,

$$\|g\|_{L^{p'}(\gamma_{\alpha p'/2})} \leq \|(\cdot, g)_\alpha\|_{(L_{hol}^p(\gamma_{\alpha p/2}))^*} \leq \left(\frac{2}{p^{1/p} p'^{1/p'}}\right)^n \|g\|_{L^{p'}(\gamma_{\alpha p'/2})}.$$

This talk will address in-progress research regarding the sharpness of the constants in the above inequality. In particular, we will demonstrate a direct relationship between the fiber over g of the projection $P_\alpha : L^p(\gamma_{\alpha p/2}) \rightarrow L_{hol}^p(\gamma_{\alpha p/2})$ and the dual norm $\|(\cdot, g)_\alpha\|_{(L_{hol}^p(\gamma_{\alpha p/2}))^*}$, a pointwise bound for functions in $L_{hol}^p(\gamma_{\alpha p/2})$, and sharpness in the first inequality given above. (Received September 22, 2012)