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Chantal David* (cdavid@mathstat.concordia.ca) and **Ethan Smith**

(ethansmith@gmail.com). *Groups of elliptic over finite fields and the Cohen-Lenstra Heuristics.*

Let G be an abelian group of rank 2 and order N , let $M_p(G)$ be the number of elliptic curves over the finite field \mathbb{F}_p with group of points isomorphic to G . We study in this talk the average of $M_p(G)$ over the prime fields \mathbb{F}_p , in particular how the average varies with the structure of the group G . We find that this variation is governed by the Cohen-Lenstra Heuristics, which predict that random abelian groups occur with probability weighted by $\#G/\#\text{Aut}(G)$ where $\text{Aut}(G)$ is the number of elements of the automorphism group of G . This variation can also be seen when we forget the group structure, and look at the average number of curves with a fixed number of points over \mathbb{F}_p .

This is joint work with E. Smith.

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