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A. Scott Duane* (adrian.duane@gmail.com) and **Jeff Remmel**. *Counting consecutive patterns in up-down permutations using the maximum packing number.*

Let A_{2n} denote the set of up-down alternating permutations of length $2n$. For a sequence of distinct integers $\sigma_1, \dots, \sigma_{2n}$, we define $red(\sigma)$ to be the sequence that results from replacing the i th smallest integer in σ by i . We say that an alternating permutation π has a τ -match at position i if $red(\pi_i, \dots, \pi_{i+2j-1}) = \tau$, where $|\tau| = 2j$. We define $\tau\text{-mch}(\sigma)$ to be the number of τ -matches in an alternating permutation σ . Furthermore, we say that τ has the *minimal overlapping property* if two τ -matches in an alternating permutation π can share at most two letters.

Let τ be an up-down alternating permutation with the minimal overlapping property. We derive the generating function

$$\sum_{n \geq 0} \frac{t^n}{n!} \sum_{\sigma \in A_{2n}} x^{\tau\text{-mch}(\sigma)} = \frac{1}{1 + \sum_{n \geq 1} \frac{t^{2n}}{(2n)!} GMP_{\tau, 2n}(x)}$$

where $GMP_{\tau, 2n}(x)$ is the *generalized maximum packing polynomial*. We define this polynomial and give examples of patterns τ for which $GMP_{\tau, 2n}(x)$, and, by extension, the generating function above, can be calculated. (Received September 25, 2012)