

1096-05-1805

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Let  $G = (V, E)$  be a graph. The *open neighborhood* of a vertex  $v \in V$  is the set  $N(v) = \{u | uv \in E\}$  and the *closed neighborhood* of  $v$  is the set  $N[v] = N(v) \cup \{v\}$ . The *open neighborhood* of set  $S$  of vertices is the set  $N(S) = \bigcup_{v \in S} N(v)$ , while the *closed neighborhood* of a set  $S$  is the set  $N[S] = \bigcup_{v \in S} N[v]$ . A set  $S \subset V$  *dominates* a set  $T \subset V$  if  $T \subseteq N[S]$ . A set  $S \subset V$  is a *dominating set* if  $N[S] = V$ ; is a *minimal dominating set* if it is a dominating set, but no proper subset of  $S$  is also a dominating set; and is a  $\gamma$ -*set* if it is a dominating set of minimum cardinality. In this paper we consider the family  $\mathcal{D}$  of all dominating sets of a graph  $G$ , the family  $\mathcal{MD}$  of all minimal dominating sets of a graph  $G$ , and the family  $\gamma$  of all  $\gamma$ -sets of a graph  $G$ . The study of these three families of sets provides new characterizations of *distance-2 domination* and *irredundance* in graphs. (Received September 16, 2013)