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Hop Dang Nguyen and **Thanh Quang Vu*** (vqthanh@math.berkeley.edu). *Koszul algebras and the Frobenius endomorphism.*

Let R be a standard graded algebra over a field of characteristic $p > 0$. Let $\varphi : R \rightarrow R$ be the Frobenius endomorphism. For each finitely generated graded R -module M , let ${}^\varphi M$ be the abelian group M with an R -module structure induced by the Frobenius endomorphism. The R -module ${}^\varphi M$ has a natural grading given by $\deg x = j$ if $x \in M_{jp+i}$ for some $0 \leq i \leq p-1$. In this talk, I will present a new criterion of Koszul algebras: R is Koszul if and only if there exists a non-zero finitely generated graded R -module M such that $\operatorname{reg}_R {}^\varphi M < \infty$. We derive this analog of Kunz's regularity criterion in positive characteristic by developing a theory of Castelnuovo-Mumford regularity over homomorphisms between \mathbb{N} -graded k -algebras, where k is a field of arbitrary characteristic. (Received September 05, 2013)