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Elizabeth A. Gillaspy* (elizabeth.a.gillaspy@dartmouth.edu), Dartmouth College,
Department of Mathematics, 27 N. Main St., Hanover, NH 03755. *The effect of homotopies of
groupoid 2-cocycles on C^* -algebraic K -theory.*

Groupoids at once generalize groups, group actions, equivalence relations, and group bundles. In his 1980 thesis, Renault explained how to construct a C^* -algebra $C^*(G, \omega)$ out of a groupoid G and a 2-cocycle $\omega \in Z^2(G, \mathbb{T})$. These twisted groupoid C^* -algebras answer many questions about the structure of other C^* -algebras, and their K -theory gives us information about D -branes in string theory.

When G is a group, Echterhoff et al. proved in 2010 that in many cases, a homotopy $\{\omega_t\}_{t \in [0,1]}$ of 2-cocycles on G leaves the K -theory groups of the twisted group C^* -algebras invariant:

$$K_*(C^*(G, \omega_0)) \cong K_*(C^*(G, \omega_1)).$$

We investigate the extent to which this K -theoretic invariance extends to the world of groupoids.

We have expanded Echterhoff et al.'s result to the case of transformation groups $G \ltimes X$; using different techniques, inspired by a 2012 result of Kumjian et al., we also show that a homotopy of 2-cocycles on the groupoid \mathcal{G}_Λ associated to a k -graph Λ induces an isomorphism

$$K_*(C^*(\mathcal{G}_\Lambda, \omega_0)) \cong K_*(C^*(\mathcal{G}_\Lambda, \omega_1)).$$

This result suggests applications to the classification of k -graph C^* -algebras. (Received September 16, 2013)