

1096-32-1725

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Craig A Nolder. *Boundary Values of Components of Monogenic Functions*.

In this paper, we study the components of monogenic functions, i.e. functions in the kernel of the Dirac Operator $D = \frac{\partial}{\partial x_0} + \sum_{i=1}^n \frac{\partial}{\partial x_i}$. Furthermore, we apply the characterization of the existence of non-tangential limits for harmonic functions in terms of their area integrals. It is a well-known fact that if u is a harmonic function in \mathbb{R}_+^3 , then for almost all $x \in \mathbb{R}^2$, the area integral,

$$S(u)(x) = \left(\int_{\Gamma(x)} |\nabla u|^2 y^{1-n} dV \right)^{\frac{1}{2}} < \infty$$

if and only if u has a non-tangential limit at x . We generalize this result for the quaternionic case. That is, for monogenic functions $u \in \mathbb{R}_+^3$ of the form

$$u = u_0 + u_1 e_1 + u_2 e_2 + u_3 e_1 e_2,$$

u_0 and u_3 have non-tangential limits almost everywhere on \mathbb{R}^2 if and only if u_1 and u_2 have non-tangential limits almost everywhere on \mathbb{R}^2 . (Received September 16, 2013)