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**Soyeun Jung\*** (soyjung@indiana.edu), 831 E 3rd St., Bloomington, IN 47405. *Pointwise asymptotic behavior of modulated periodic reaction-diffusion waves.*

We discuss, under standard spectral stability assumptions, pointwise stability and asymptotic behavior of localized modulated spatially periodic traveling waves  $u(x, t) = \bar{u}(x - at)$  of systems of reaction-diffusion equations of form  $u_t = u_{xx} + f(u)$ , where  $(x, t) \in \mathbb{R} \times \mathbb{R}^+$ ,  $u \in \mathbb{R}^n$ , and  $f : \mathbb{R}^n \rightarrow \mathbb{R}^n$  is sufficiently smooth. By working with the periodic resolvent kernel and the Bloch-decomposition, we first establish pointwise bounds for the Green function of the linearized equation associated with  $\bar{u}$ . With our linearized estimates together with a nonlinear iteration scheme developed by Johnson-Zumbrun, we obtain pointwise asymptotic behavior of periodic traveling waves  $\bar{u}(x)$  by showing that perturbations of  $\bar{u}(x)$  converge to the heat kernel under small initial perturbations,  $|u_0| \leq E_0 e^{-|x|^2/M}$  with  $|u_0|_{H^2} \leq E_0$ , and  $|u_0| \leq E_0(1 + |x|)^{-r}$ ,  $r > 2$  with  $|u_0|_{H^2} \leq E_0$  respectively, where  $E_0 > 0$  sufficiently small and  $M > 0$  sufficiently large. Here, we emphasize again that it is the pointwise description that is the main new aspect of our research. (Received August 30, 2013)