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**William B. Johnson\*** ([johnson@math.tamu.edu](mailto:johnson@math.tamu.edu)), Department of Mathematics, Texas A&M University, College Station, TX 77845-3368. *Embeddings of  $\ell_p(\aleph)$  into  $L_p$  spaces.* Preliminary report.

Gideon Schechtman and I prove that if  $X$  is a subspace of an  $L_p$  space,  $1 < p < 2$ , and  $\ell_p(\aleph_1)$  does not embed into  $X$ , then  $X$  embeds into  $L_p(\mu)$  for some finite measure  $\mu$ . We also give appropriate versions of this result for  $\ell_p(\aleph)$  with  $\aleph$  any uncountable cardinal. The  $\aleph_1$  result complements a theorem proved by P. Enflo and H. P. Rosenthal 40 years ago; namely, that  $\ell_p(\aleph_1)$ ,  $1 < p < 2$ , does not (isomorphically) embed into  $L_p(\mu)$  with  $\mu$  a finite measure.

This work is an outgrowth of an unsuccessful attempt to solve a problem left open by Enflo and Rosenthal; namely, whether  $L_p(\mu)$  can have an unconditional basis when  $1 < p \neq 2 < \infty$ , the measure  $\mu$  is finite, and the density character of  $L_p(\mu)$  is  $\aleph_1$ . If the answer is yes, then the results of Enflo and Rosenthal would show that “ $L_p(\{-1, 1\}^{2^{\aleph_0}})$  has an unconditional basis” is undecidable. (Received September 15, 2013)