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Diffusion approaches have been used in the last several years to describe and analyze the underlying geometry of a given data set. One starts by constructing a diffusion matrix—a Markov matrix modeling discretized heat flow (or possibly a nearest neighbor random walk) on the data. The eigenvalues and eigenvectors of this matrix (or its symmetric version) can be used to build an isometric embedding of the data points. This isometry is expressed in the  $l_2$  metric, and often leads to  $l_2$  being used in defining a related diffusion distance. However,  $l_2$  does not seem very natural for this situation since the rows of the diffusion matrix are probability densities which are normalized in  $l_1$ . Another indication that  $l_1$  is more desirable than  $l_2$  arises from considering the continuous case situation of heat flow in  $n$ -dimensional Euclidean space. An  $L_2$  analog gives rise to Euclidean distance with time scale dependent on the dimension  $n$ , while an  $L_1$  analog involves Euclidean distance with time scale independent of  $n$ , which seems intrinsically more desirable.

In this talk we present our investigation of defining and exploring the properties of  $l_1$ -based diffusion distances. (Received September 17, 2013)