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*Upset-downset*. Preliminary report.

Let  $P$  be a finite poset. For  $x \in P$ , recall that the *downset* and *upset* of  $x$  are defined to be  $\tilde{x} = \{y \in P \mid y \leq x\}$  and  $\hat{x} = \{y \in P \mid y \geq x\}$ , respectively. We define the *upset-downset game*  $G(P)$  to be the game with the following possible moves: For any  $x \in P$ , **Left** may remove the downset of  $x$ , leaving the game  $G(P - \tilde{x})$ ; and for any  $x \in P$ , **Right** may remove the upset of  $x$ , leaving the game  $G(P - \hat{x})$ . The first player unable to move loses, i.e.,  $G(\emptyset) = 0$ . By standard results, we see that upset-downset is a partizan game whose values are all infinitesimal (“all small”).

This talk describes our work in two special cases of upset-downset. In the case where the Hasse diagram of  $P$  is a disjoint union of complete bipartite graphs, we exhibit a winning strategy for any winnable position. We also describe preliminary results in the case where  $P$  is a rank 2 poset where the downset of every rank 2 element  $x$  contains exactly two elements of rank 1. (Such posets may be thought of as graphs, where the rank 2 elements come from edges and the rank 1 elements come from vertices.) (Received September 17, 2013)