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*Properties of the  $(a, b)$ -Fibonacci Sequence, Modulo  $m$ .*

For integers  $a$  and  $b$ , we consider the  $(a, b)$ -Fibonacci sequence  $F$  defined by  $F_0 = 0$ ,  $F_1 = 1$ , and  $F_n = aF_{n-1} + bF_{n-2}$ .  $F \pmod{m}$  is periodic with period denoted  $\pi(m)$ . The rank of  $F \pmod{m}$ , denoted  $\alpha(m)$ , is the least positive  $r$  such that  $F_r \equiv 0 \pmod{m}$ , and the order of  $F \pmod{m}$ , denoted  $\omega(m)$ , is  $\pi(m)/\alpha(m)$ . We pull together results on  $\pi(m)$ ,  $\alpha(m)$ , and  $\omega(m)$  from the classic case  $a = 1$ ,  $b = 1$ , and generalize them to accommodate arbitrary integers  $a$  and  $b$ . Matrix methods are used to provide elementary proofs. (Received September 17, 2013)