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**Christopher Coscia\*** (cosciach@bc.edu) and **Jonathan DeWitt**. *Locally Convex Words and Permutations.*

Define a *k-convex permutation*  $\pi : [n] \rightarrow [n]$  to be a bijection obeying the condition  $2\pi(i) \geq \pi(i-1) + \pi(i+1) - k$  for all  $i \in \{2, 3, \dots, n-1\}$  for fixed  $k \geq 0$ , and denote the number of *k-convex permutations* of length  $n$  by  $f_k(n)$ . We attempt to determine  $f_k(n)$  for  $k = 0, 1$ , and  $2$ , cases under which these permutations satisfy nice properties; in particular, they are consecutive 213 and 312 avoiding. We show that  $f_0(n)$  is precisely 8 for  $n > 4$  and demonstrate, for  $k = 1, 2$ , a method of exhaustively constructing *k-convex permutations*. We construct an infinite "descendant digraph" for  $k = 1$  and  $k = 2$ , and use the transfer matrix method with generating functions to determine  $f_1(n)$ , give a partial solution for  $f_2(n)$ , and demonstrate that it is possible to give arbitrarily tight exponential bounds in both cases.

Similarly, we define *k-convex words on a p-alphabet* to be functions  $g : [n] \rightarrow [p]$  satisfying  $2g(i) \geq g(i-1) + g(i+1) - k$  for all  $i \in \{2, 3, \dots, n-1\}$ . We demonstrate that it is possible to find a generating function  $G_{p,k}$  for any values of  $p, k$ , and show that the number of 0-convex words is eventually constant in  $n$  for any  $p$ , giving an expression for this constant in  $p$  related to the integer partition numbers. (Received September 09, 2014)