

1106-05-2087

**David Rolnick** (drolnick@math.mit.edu) and **Praveen S. Venkataramana\***  
(venkap@mit.edu). *On the growth of Stanley sequences.*

A set is said to be *3-free* if no three elements form an arithmetic progression. Given a 3-free set  $A$  of integers  $0 = a_0 < a_1 < \dots < a_t$ , the *Stanley sequence*  $S(A) = \{a_n\}$  is defined using the greedy algorithm: For each successive  $n > t$ , we pick the smallest possible  $a_n$  so that  $\{a_0, a_1, \dots, a_n\}$  is 3-free and increasing. Work by Odlyzko and Stanley indicates that Stanley sequences may be divided into two classes. Sequences of Type 1 are highly structured and satisfy  $\alpha n^{\log_2 3}/2 \leq a_n \leq \alpha n^{\log_2 3}$ , for some constant  $\alpha$ , while those of Type 2 appear chaotic and satisfy  $\Theta(n^2/\log n)$ . In this paper, we consider the possible values for  $\alpha$  in the growth of Type 1 Stanley sequences. Whereas Odlyzko and Stanley assumed that  $\alpha = 1$ , we show that  $\alpha$  can be any rational number that is at least 1 and for which the denominator, in lowest terms, is a power of 3. (Received September 15, 2014)