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Nicholas A. Loehr* (nloehr@vt.edu), Virginia Tech Dept. of Mathematics, 460 McBryde Hall, Blacksburg, VA 24061-0123, and **Drew Armstrong** and **Gregory S. Warrington**. *Binomial coefficients, rational Catalan numbers, and their q -analogues*. Preliminary report.

Binomial coefficients count lattice paths contained in rectangles, whereas Catalan numbers (and their generalizations, the *rational* Catalan numbers) count lattice paths contained in certain triangles. The q -binomial coefficients enumerate lattice paths based on either their inversion count or their major index; these two combinatorial statistics lead to two distinct q -analogues of Catalan numbers. A long-standing open problem is to find a combinatorial statistic to explain the natural algebraic q -analogue of the rational Catalan numbers. We conjecture such a combinatorial statistic along with a novel combinatorial interpretation for the q -binomial coefficients. We give a bijective proof that the new formula for q -binomial coefficients implies the conjecture for q -Catalan numbers. (Received August 24, 2014)