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Comlan de Souza* (csouza@csufresno.edu). *Characterization of self dual lattices in \mathbb{R}, \mathbb{R}^2 , and \mathbb{R}^3 .*

Consider the linearly independent sets of real n (column) vectors a_1, \dots, a_n and the lattice generated by these vectors

$$\mathcal{L}_A := \left\{ \sum_{k=1}^n m_k a_k : m_1, \dots, m_n \in \mathbb{Z} \right\}$$

where A is the matrix formed by these column vectors. The lattice $\mathcal{L}_{A^{-T}}$ generated by vectors biorthogonal to a_1, \dots, a_n is said to be the dual of the lattice \mathcal{L}_A . Moreover \mathcal{L}_A is said to be self dual if and only if

$$(A^{-T})^{-1}A = A^T A$$

is a matrix of integers with determinant ± 1 . We will show by an ad-hoc method, that the only self dual lattices in $\mathbb{R}, \mathbb{R}^2, \mathbb{R}^3$ are rotations of $\mathbb{Z}, \mathbb{Z} \times \mathbb{Z}$, and $\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z}$. (Received September 15, 2014)