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**Ashvin Anand Swaminathan\*** (aaswaminathan@college.harvard.edu), 388 Eliot Mail Center, Harvard College, 101 Dunster Street, Cambridge, MA 02138. *On Arboreal Galois Representations of Rational Functions.*

The action of the absolute Galois group  $\text{Gal}(K^{\text{sep}}/K)$  of a global field  $K$  on a tree  $T(\phi, \alpha)$  of iterated preimages of  $\alpha \in \mathbb{P}^1(K)$  under  $\phi \in K(x)$  with  $\deg(\phi) \geq 2$  induces a homomorphism  $\rho : \text{Gal}(K^{\text{sep}}/K) \rightarrow \text{Aut}(T(\phi, \alpha))$ , called an arboreal Galois representation. We address questions of Jones and Manes about the size of  $G(\phi, \alpha) := \text{im}\rho$ . We consider two cases: (1)  $\phi$  is such that  $\{a_n\}$  defined by  $a_0 = \alpha$  and  $a_n = \phi(a_{n-1})$  is periodic, and (2)  $\phi$  commutes with a nontrivial Möbius transformation that fixes  $\alpha$ .

In the first case, we resolve a question of Jones about the size of  $G(\phi, \alpha)$ , and taking  $K = \mathbb{Q}$ , we describe the Galois groups of iterates of  $\phi \in \mathbb{Z}[x]$  when  $\phi(x) = x^2 + kx$  or  $\phi(x) = x^2 - (k+1)x + k$ . Taking  $\phi(x) = x^2 + kx \in \mathbb{Z}[x]$ , we employ a result of Jones regarding the size of the group  $G(\psi, 0)$ , where  $\psi(x) = x^2 - kx + k$ , to obtain a zero-density result for primes dividing terms of  $\{a_n\}$ . In the second case, we resolve a conjecture of Jones about the size of a certain subgroup  $C(\phi, \alpha) \subset \text{Aut}(T(\phi, \alpha))$  that contains  $G(\phi, \alpha)$ . (Received September 10, 2014)