Let $X$ be a completely regular Hausdorff space, and $\mathcal{D}$ a cover of $X$. Mati Abel, J. Arhippainen, and J. Kauppi in [Mediterr. J. Math. 7 (2010) 271-282] and [Cent. Eur. J. Math. 10 (2012), 1060-1066] describe the cover-strict topology on $C_b(X, \mathcal{D})$, the space of continuous scalar-valued functions on $X$ which are bounded on each $D \in \mathcal{D}$, and investigate the ideal and quotient structures of $C_b(X, \mathcal{D})$. We use ideas from the theory of bundles of topological vector spaces (in particular, bundles of Banach spaces and Banach algebras), as found in e.g. G. Gierz [Lect. Notes Math. 955 (Springer-Verlag, 1982)] and the present authors’ papers [Acta Comment. Univ. Tartuensis Math. 14 (2010), 75-90] and [Quaest. Math. 34 (2011), 361-376] to define analogous topologies on section spaces of such bundles, and to discuss completeness properties, ideals, and quotients of such spaces. (Received September 03, 2014)