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*Multiresolutions.*

Multi-scale analyses and multiresolutions in multivariate signal analysis offer fast algorithms which also have strong localization properties. The latter feature makes them useful as wavelet algorithms as well; i.e., for building recursive basis constructions from filter banks and multi-resolutions in Hilbert spaces, yielding much better pointwise approximation properties than traditional Fourier bases. In the talk we present a new approach to subdivision of signals into frequency bands, applicable to modern-day wireless transmission. We present a representation theoretic framework for perfect reconstruction filter-banks: via a representation theory create the Hilbert spaces  $H$ , and subspaces in  $H$ , in such a way that "non-overlapping frequency bands" correspond to orthogonal subspaces in  $H$ ; or equivalently to systems of orthogonal projections. Different frequency bands must exhaust the signals for the entire system, the orthogonal projections add to the identity operator in  $H$ . We select special families of commuting orthogonal projections in  $H$  via an iteration of the initial generators and repeated subdivision sequences. (Received September 11, 2014)