

1106-94-2908

**Igor Zelenko\***, zelenko@math.tamu.edu, **Muxi Yan**, mxyan@tamu.edu, **Alex Sprintson**, spalex@tamu.edu, and **Swanand Kadhe**, kswanand1@tamu.edu. *On MDS Codes with Constrained Generator Matrices and Related Problems.*

Our aim is to design generator matrices of Maximum Distance Separable (MDS) codes such that each row of the generator matrix has a specific support. More specifically, we consider an  $(n, k)$ -MDS code for which each row of its generator matrix contains up to  $k - 1$  zeros at certain places, and the elements at the remaining places can be assigned any values from the underlying finite field. We call such a generator matrix as the constrained generator matrix  $G_{con}$ . It can be shown that if  $G_{con}$  does not contain an  $l \times m$  zero sub-matrix such that  $l + m = k + 1$ , then randomly choosing the values of non-zero elements over a finite field of sufficiently large size results in an MDS code with high probability. We say that  $G_{con}$  is feasible if it is possible to complete it to an MDS code. We conjecture that it is possible to linearly transform a Vandermonde matrix to obtain the constrained generator matrix with high probability for any feasible matrix  $G_{con}$ . We verify this conjecture for a large number of cases. This conjecture admits a number of reformulations that lead to interesting conjectures in algebraic geometry, abstract algebra and number theory. In particular, our method to verify it is based on a purely geometric reformulation of the problem. (Received September 17, 2014)