Ken Ono*, Emory University, Atlanta, GA 30332. *Golden numbers and identities: The legacy of Rogers and Ramanujan.

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