

1106-VN-1777

Brent Moran* (brent.moran@ucdenver.edu), **Matt Mowrey**
(matthew.mowrey@ucdenver.edu) and **Michael Ferrara** (michael.ferrara@ucdenver.edu).

Ramsey-Minimal Saturation Numbers for Sets of Stars.

A graph G is \mathcal{F} -saturated for a family \mathcal{F} of graphs if G contains no member of \mathcal{F} as a subgraph, but for any edge $e \in E(\overline{G})$, some member of \mathcal{F} is a subgraph of $G + e$. The *saturation number* $\text{sat}(n, \mathcal{F})$ is the minimum number of edges in an \mathcal{F} -saturated graph of order n . If $\mathcal{F} = \{F\}$ for a single graph F , we say G is F -saturated, denoted $\text{sat}(n, F)$.

Given a set $\{H_1, \dots, H_k\}$ of graphs, a graph G is called (H_1, \dots, H_k) -Ramsey-minimal if every k -coloring of $E(G)$ contains some H_i in color i , but for any edge $e \in E(G)$, some k -coloring of $G - e$ does not. We denote the family of (H_1, \dots, H_k) -Ramsey-minimal graphs by $\mathcal{R}_{\min}(H_1, \dots, H_k)$.

Motivated in part by a 1987 conjecture of Hanson and Toft, we prove a number of results about Ramsey-minimal saturation numbers for sets of stars. In particular, we give an upper bound on $\text{sat}(n, \mathcal{R}_{\min}(K_{1,t_1}, \dots, K_{1,t_p}))$ for arbitrary t_1, \dots, t_p , and show that it is sharp when $p = 2$ and in several other cases. (Received September 15, 2014)