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**Nathaniel Karst, Jessica Oehrlein\*** ([jessica.oehrlein@students.olin.edu](mailto:jessica.oehrlein@students.olin.edu)), **Denise Sakai Troxell** and **Junjie Zhu**. *Distance Labelings of Amalgamations and Injective Labelings of General Graphs*.

An  $L(2,1)$ -labeling of a graph  $G$  is a function assigning a non-negative integer to each vertex such that adjacent vertices are labeled with integers differing by at least 2 and vertices at distance two are labeled with integers differing by at least 1. The minimum span across all  $L(2,1)$ -labelings of  $G$  is denoted  $\lambda(G)$ . An  $L'(2,1)$ -labeling of  $G$  and the number  $\lambda'(G)$  are defined analogously, with the additional restriction that the labelings must be injective. We determine  $\lambda(H)$  where  $H$  is a join-page amalgamation of graphs which is defined as follows: given  $p \geq 2$ ,  $H$  is obtained from the pairwise disjoint union of graphs  $H_0, H_1, \dots, H_p$  by adding all the edges between a vertex in  $H_0$  and a vertex in  $H_i$  for  $i = 1, 2, \dots, p$ . Motivated by these join-page amalgamations, we show that  $\lambda'(G) = \max\{n - 1, \lambda(G)\}$ , where  $n$  is the number of vertices in  $G$ . (Received August 13, 2014)