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**Shyam S. Narayanan\*** ([shyam.s.narayanan@gmail.com](mailto:shyam.s.narayanan@gmail.com)), 8209 W 143rd Ter, Overland Park, KS 66223. *Improving the Speed and Accuracy of the Miller-Rabin Primality Test*. Preliminary report.

Currently, even the fastest deterministic primality tests run too slowly, with the Agrawal-Kayal-Saxena (AKS) primality test runtime  $\tilde{O}(\log^6(n))$ , and probabilistic primality tests are still highly inaccurate. In this paper, we discuss the accuracy of the Miller-Rabin Primality Test and the number of non-witnesses for a general composite odd integer  $n$ . We also extend the Miller-Rabin Theorem by determining when the number of non-witnesses  $N(n)$  equals  $\frac{\varphi(n)}{4}$  and by proving that for all  $n$ , if  $N(n) > \frac{5}{32} \cdot \varphi(n)$  then  $n$  must be of one of the following 3 forms:  $n = (2x + 1)(4x + 1)$ , where  $x$  is an integer,  $n = (2x + 1)(6x + 1)$ , where  $x$  is an integer,  $n$  is a Carmichael number of the form  $pqr$ , where  $p, q, r$  are distinct primes congruent to 3 (mod 4). Finally, we find witnesses to certain forms of composite numbers with high rates of nonwitnesses. This work is expected to result in a faster and better primality test for large integers. (Received September 16, 2014)