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Let  $G$  be a Polish group.  $G$  is algebraically determined Polish group if given any Polish group  $L$  and an algebraic isomorphism  $\varphi : L \rightarrow G$ , then  $\varphi$  is a topological isomorphism. Let  $N$  and  $H$  be two Polish groups and let  $\theta : H \rightarrow \text{Aut}(N)$  be a group homomorphism that satisfies  $N \times H \rightarrow N$ ,  $(n, h) \rightarrow \theta_h(n)$  is continuous. Then  $N \rtimes_{\theta} H$  is a Polish group in the product topology. Let  $L$  be a Polish group and let  $\varphi : L \rightarrow N \rtimes_{\theta} H$  be a group isomorphism. If  $\varphi^{-1}(N)$  and  $\varphi^{-1}(H)$  are both analytic subgroups of  $L$ , then both  $\varphi^{-1}(N)$  and  $\varphi^{-1}(H)$  are closed subgroups of  $L$ . Next, if  $\varphi|_{\varphi^{-1}(N)} : \varphi^{-1}(N) \rightarrow N$  is measurable with respect to  $BP(\varphi^{-1}(N))$ , then  $\varphi|_{\varphi^{-1}(N)}$  is a topological isomorphism. Furthermore, if, in addition,  $\theta$  is injective, then  $\varphi|_{\varphi^{-1}(H)} : \varphi^{-1}(H) \rightarrow H$  is a topological isomorphism. Finally, under all of these conditions,  $\varphi : L \rightarrow N \rtimes_{\theta} H$  is a topological isomorphism and thus  $N \rtimes_{\theta} H$  is an algebraically determined Polish group. Now we will apply the above theorem on the natural semidirect product  $R^n \rtimes G(n)$ . (Received September 11, 2014)