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Inspired by the Fibonacci identity  $f_{n-1} \times f_{n+1} + 1 = f_n^2$  for odd  $n$ , we define a relation  $\sim$  on  $\mathbb{N}$  by  $a \sim b$  if and only if  $ab + 1 = k^2$  for some  $k$ .  $\sim$  is obviously symmetric but not reflexive nor transitive. The relation results in an undirected graph  $G$  with vertex set  $\mathbb{N}$  and an edge between  $a$  and  $b$  if  $a \sim b$ . We investigate the neighbor sets  $N(a) = \{x \in \mathbb{N} \mid a \sim x\}$  and the upper bounds for the distance  $d(a, x) = \min\{\text{length of paths from } a \text{ to } x\}$  for special  $a \in \mathbb{N}$ . We also look into triples  $(a, b, c)$  with  $a \sim b, b \sim c$ , and  $c \sim a$  and the resulting cycles on the graph. (Received September 11, 2014)