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**Stephen M. Gagola III\*** (gagolasm@miamioh.edu), Department of Mathematics, Miami University, Oxford, OH 45056. *Multiplicative properties of partitions of integers.*

Here we give a combinatorial proof of an inequality that was first proven by Christine Bessenrodt and Ken Ono. Bessenrodt and Ono proved that the number of partitions of  $n$ , say  $p(n)$ , satisfies  $p(a)p(b) > p(a+b)$  for  $a, b > 1$  and  $a+b > 9$  by using a result of Lehmer and asked whether a combinatorial proof exists. Here we prove the inequality combinatorially and show that the proof can also be extended to prove the analogous inequality for  $k$ -regular partitions with  $k \geq 2$ . For  $2 \leq k \leq 6$ , these inequalities were first proven to hold for  $k$ -regular partitions by Olivia Beckwith and Christine Bessenrodt using similar methods to the  $p(n)$  case. (Received September 20, 2016)