

1125-05-2986

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*Games on Graphs: Seepage!* Preliminary report.

The game of Seepage, first described by Clarke, et al. in 2009, is played by two players, Sludge,  $S$ , and Green,  $G$ , on a directed acyclic graph with a single source and several sinks.  $S$  and  $G$  alternately claim vertices of the graph, which subsequently cannot be claimed by the opponent. Sludge begins by claiming, or 'contaminating', the source. Afterwards, in sequence,  $G$  can claim, or 'protect', any vertex on the graph, while  $S$  can contaminate any vertex adjacent to an already contaminated vertex.  $S$  is said to win if any sink is contaminated; otherwise,  $G$  wins. The generalized version of this game allows  $G$  to claim multiple vertices each turn. The *green number* of a graph  $H$ ,  $gr(H)$ , is defined to be the minimum  $k$  such that  $G$  can guarantee victory with at most  $k$  moves on each turn. Graphs are called *green-win* if  $gr(H) = 1$ , *sludge-win* if  $gr(H) > 1$  and *k-green-win* if  $gr(H) = k$ . In their paper, Clarke, et al. characterized green-win and k-green-win rooted trees  $T$ , providing a polynomial time algorithm for determining if  $gr(T) = k$ . We introduce a more generalized algorithm that determines if  $gr(H) = k$  for any directed acyclic graph, as well as methods to reduce the number of vertices and edges of a graph without changing the green number. (Received September 20, 2016)