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**JiYoon Jung\*** (jungj@marshall.edu), **Suhyung An** and **Sangwook Kim**. *Enumeration of  $k$ -Fuss-Catalan paths and  $(k, r)$ -Fuss-Schröder paths*. Preliminary report.

In this paper we provide three results involving  $k$ -Fuss-Catalan paths and  $(k, r)$ -Fuss-Schröder paths. First, we enumerate the number of  $k$ -Fuss-Catalan paths of type  $\lambda$ . J. H. Przytycki and A. S. Sikora studied  $k$ -Fuss-Catalan paths of length  $n$ , and we extend the study to  $k$ -Fuss-Catalan paths with type  $\lambda$  and  $m$  connected components. By taking the sum over  $m$  we get the number of  $k$ -Fuss-Catalan of type  $\lambda$ . Second, we enumerate the number of  $(k, r)$ -Fuss-Schröder paths of type  $\lambda$ . Y. Park and S. Kim studied Schröder paths with type  $\lambda$  and  $m$  connected components. Generalizing the results to  $(k, r)$ -Fuss-Schröder paths we give a combinatorial interpretation for the number of small  $(k, r)$ -Fuss-Schröder paths of type  $\lambda$  by using Chung-Feller style. We also give explicit formula for the number of large  $(k, r)$ -Fuss-Schröder paths of type  $\lambda$  with  $d$  diagonal steps touching the line  $y = kx$ , and a description for the number of all large  $(k, r)$ -Fuss-Schröder paths of type  $\lambda$ . Finally, we find two sets of sparse noncrossing partitions of  $[2(k+1)n+1]$  which are in bijection with the set of all small (respectively, large)  $(k, r)$ -Fuss-Schröder paths of type  $\lambda$ . (Received September 20, 2016)