

1125-05-632

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Marcantonio and Mohamed Omar.** *Peak Sets of Graphs.*

If  $G$  is a connected graph with  $n$  vertices denoted  $v_0, \dots, v_{n-1}$ , then a permutation of length  $n$  corresponds to a labeling (or  $n$ -coloring) of the vertices of  $G$ . We say that a permutation  $\pi$  has a peak at the vertex  $v_i$  on  $G$  if the label of  $v_i$  is greater than all of the labels of  $v_i$ 's neighboring vertices, with the caveat that we do not allow peaks at vertices of degree 1 or 0, as these are more like cliffs than peaks. The  $G$ -peak set of a permutation  $\pi$  is defined to be the set  $P_G(\pi) = \{i \in [n] : \pi \text{ has a peak at the vertex } v_i\}$ , where  $[n] = \{1, 2, 3, \dots, n\}$ . Given a subset  $S \subseteq V(G)$  we denote the set of all permutations with  $G$ -peak set  $S$  by  $\mathcal{P}_S(G) = \{\pi \in \mathfrak{S}_n \mid P_G(\pi) = S\}$ . We note that the peaks sets  $P_S(n)$  originally studied by Billey, Burdzy, and Sagan corresponded to studying peak sets on the path graph  $P_n$ , i.e.,  $P_S(n) = \mathcal{P}_S(G)$  where  $G = P_n$ . In this talk, we present a recursive formula for enumerating  $|\mathcal{P}_S(G)|$  and provide closed formulas for the number of permutations with a given peak set for a collection of interesting families of graphs. (Received September 08, 2016)