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Robert Erra*, 14-16 rue Voltaire, 94270 Le Kremlin Bicetre, France, and **Marwan Burelle**,
Alexandre Letois and **Mark Angoustures**. *A new spectral graph entropy*. Preliminary report.

We propose here a new graph entropy. Let G be an undirected graph of size N ; the now classical Von Neumann entropy of a graph is defined as: $S(G) = -\sum_{i=1}^N \lambda_i \log(\lambda_i)$, with $Sp(G) = \{\lambda_1, \dots, \lambda_N\}$ the spectrum of the adjacency matrix of G ; we can also use the spectrum of the normalized combinatorial Laplacian of G .

Let k be the number of distinct eigenvalues, let $M = \{m_1, \dots, m_k\}$ be the vector of multiplicities of all eigenvalues and let $\mathcal{M} = \{\omega_1 = m_1/N, \dots, \omega_k = m_k/N\}$ be the normalized vector of multiplicities. So we have $\sum_{i=1}^k \omega_i = 1$, we can then compute $H_S(G) = -\sum_{i=1}^k \omega_i \log(\omega_i)$, and we will call this the *spectral graph entropy*. This is the Shannon entropy of the normalized vector of eigenvalue multiplicities.

This entropy has a nice property: it can be computed for directed or undirected graphs, for weighted or unweighted graphs. We can also compute the graph entropy with the normalized combinatorial Laplacian of G instead of using the adjacency matrix.

We will present a simple algorithm to compute exactly this spectral entropy. We will give some of its properties and we will present some open problems. (Received September 20, 2016)