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John M. Dusel* (jdusel@whittier.edu), Department of Mathematics, Whittier College, 13406 Philadelphia St., Whittier, CA 90608. *Crystal folding*.

We introduce a procedure to fold a crystal B of simply-laced Cartan type \mathcal{C} by the action of an automorphism σ , which produces a crystal B_σ for the folded Langlands dual datum $\mathcal{C}^{\sigma^\vee}$. This construction preserves normality and the Weyl group action, and is compatible with Kashiwara's tensor product rule.

Combinatorial properties of the folding of $B(\infty)$ reflect the structure of subalgebra of the quantum group $U_q^-(\mathcal{C})$. In particular, this subalgebra admits a $U_q^-(\mathcal{C}^{\sigma^\vee})$ -module structure via Berenstein and Greenstein's machinery of quantum folding, which is encoded by the $\mathcal{C}^{\sigma^\vee}$ -crystal structure of $B(\infty)_\sigma$. We find that $B(\infty)_\sigma$ is generated by a *set* of highest-weight elements over the monoid of lowering operators. The highest-weight set of $B(\infty)_\sigma$ identifies with a monoid admitting a unique finite \subset -minimal generating set, in finite type, and a subset of the Weyl group called the balanced parabolic quotient is in one-to-one correspondence with this generating set in type D . (Received September 19, 2016)