Let $G$ be a simple algebraic group over an algebraically closed field of prime characteristic $p$ which is split over the prime field. If $p$ is roughly twice the size of the Coxeter number or larger it is well-known that the tensor product of a Steinberg module and any simple $G$-module with restricted highest weight is a tilting module. Not much is known about these tensor products for smaller primes. This question is of interest because it is closely related to two long-standing conjectures by Stephen Donkin. The first concerns the lifting of projective modules of the Frobenius kernels to $G$. The second deals with various types of filtrations and their connection. This talk is a survey of known results together with explicit examples. (Received September 19, 2016)