This is an ongoing joint work with Clifford J. Earle. Let $V$ be a simply connected complex Banach manifold with a basepoint. Let $G$ be a subgroup of $\text{PSL}(2,\mathbb{C})$, $E$ be a subset of the Riemann sphere (containing at least 3 points), and suppose that $E$ is invariant under $G$. In this talk, we will discuss a new result on holomorphic families of isomorphisms of $G$. Our result crucially depends on the conformal naturality and real-analyticity of “Douady-Earle” sections (also called “barycentric sections”) of some generalized Teichmüller spaces. (Received September 12, 2016)