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**Jerome Goddard II, Quinn Morris\*** (qamorris@uncg.edu), **Catherine Payne, Jordan Price and R. Shivaji.** *Analysis of steady states for classes of reaction-diffusion equations with U-shaped density dependent dispersal on the boundary.*

We consider positive solutions to equations of the form

$$\begin{cases} -\Delta u = \lambda u(1 - u), & x \in \Omega, \\ \frac{\partial u}{\partial \eta} + \gamma \sqrt{\lambda}(u - A)^2 u = 0, & x \in \partial\Omega, \end{cases}$$

where  $\lambda > 0, \gamma > 0, A \in (0, 1)$  are parameters,  $\Omega$  is a bounded domain in  $\mathbb{R}^n$ ;  $n \geq 1$  with smooth boundary  $\partial\Omega$  and  $\frac{\partial u}{\partial \eta}$  is the outward normal derivative. Such models arise in the study of population dynamics in a habitat  $\Omega$  when the population exhibits U-shaped density dependent dispersal on the boundary. We analyze the persistence of the population (existence, non-existence, uniqueness and multiplicity of positive solutions) as the patch size ( $\lambda$ ) and the hostility of the outside matrix ( $\gamma$ ) vary. We obtain results when  $\Omega = (0, 1)$  via a quadrature method, and when  $\Omega$  is any bounded domain in  $\mathbb{R}^n$ ;  $n > 1$  by the method of sub-super solutions. (Received September 14, 2016)