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The orbital stability of standing-wave solutions to the non-linear Schrödinger equation

$$i\partial_t\varphi(t, x) + \Delta_x\varphi(t, x) - G(\varphi(t, x)) = 0$$

follows from properties of the set of minima of the functional

$$E(u) = \frac{1}{2} \int_{\mathbb{R}^n} |\nabla u(x)|^2 dx + \int_{\mathbb{R}^n} G(u(x)) dx$$

on the constraint  $S = \{u \in H_{r,+}^1(\mathbb{R}^n) \mid \|u\|_{L^2}^2 = 1\}$ . The functions  $H_{r,+}^1(\mathbb{R}^n)$  are radially symmetric (with respect to the origin),  $H^1$  and positive. Stability holds when this set is finite. It is known from Kwong (ARMA, 1989) and Berestycki and Lions (ARMA 1983) that if  $G(s) = -a|s|^p$ , there is exactly one minimum. We show that this uniqueness holds for combined power-type non-linearities,  $G(s) = -a|s|^p + b|s|^q$  and spatial dimension  $n = 1$ . We also provide a condition on  $G$  ensuring that minima of  $E$  on  $S$  are non-degenerate. As a consequence, there are only finitely many of them. (Received September 20, 2016)