

1125-40-2461

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William McDermott (willm97@vt.edu) and **Alex Wilson** (wils1256@msu.edu). *Classification of numerical sequences originating from recursive polynomial sequences*. Preliminary report.

In this talk, we classify the asymptotic behavior of sequences which can be generated from polynomials which satisfy the following recurrence relation:

$$\begin{cases} M_n(x, y) = xM_{n-1}(x, y) + yM_{n-2}(x, y) & n \geq 2 \\ M_0 = a \\ M_1 = bx + cy + d \end{cases}$$

where a, b, c , and d are real constants. We present a Binet formula for M_n , which allows us to classify these sequences using a triangle in \mathbb{R}^2 . The sequence $M_n(x, y)$ evaluated inside the triangle converges to zero, while $M_n(x, y)$ evaluated outside the triangle diverges. We also discuss subtle behaviors on the boundary such as periodicity and convergence to a constant. Moreover, we present a finite sum expression for M_n , which can be used to generate sequences that we interpret combinatorially. One example we provide a combinatorial proof for is

$$\sum_{k=0}^{\lfloor \frac{n+1}{2} \rfloor} \left[\binom{n-k}{k} + (w-1) \binom{n-k-1}{k} \right] w^k (w-1)^k = w^n$$

Finally, we explain how the first derivative of M_n with respect to y under certain conditions generates sequences that are typically found by convolution of two numerical sequences. (Received September 20, 2016)