I will discuss various conditions that imply when a non-degenerate bivariate measure supported on the square is absolutely continuous with respect to Lebesgue measure with a density that is the reciprocal of a positive polynomial. Such measures are called Bernstein-Szego measures. This is joint work with Plamen Iliev. (Received September 19, 2016)