

1125-VK-3023      **Mojtaba Moniri\*** (m-moniri@wiu.edu). *Pairs of close cycle-points in a logistic map:  
5-periodicity or 10?*

The logistic map with parameter  $r$  is defined on  $[0, 1]$  as  $f_r(x) = rx(1 - x)$ . Most parameters  $r \in (3.570, 4)$  exhibit a chaotic orbit for an arbitrary initial point  $x_0 \in (0, 1)$ . However the interval  $(3.739, 3.744)$  is inside a period-5, 10, 20, 40, etc., region (with successive period-doubling bifurcations). Here we are concerned with the particular parameter  $r = 3.74$  to clarify on some misleading literature, like half of a dozen items which we mention, that claim an attracting 5-cycle. For  $x_0 = 0.5$ , some relied on, just as early as, the 100 – 110th terms, all up to only six decimal digits. We give a Mathematica code which outputs the 100,000,000th term followed by the next 19, all with 22 digits (in  $\approx 3$  minutes on an ordinary desktop). It indicates two cycles of length 10. The five pairs of counterpart numbers agree up to 13 – 15 digits. Generally speaking, and in similar situations, one could challenge this via two attacking approaches. One is to iterate more in an effort to see if we can overcome disagreements: can the digits be stabilized and discrepancies go away (10 to 5 undertake)? In parallel, one can zoom out on the digits in an effort to see if the current agreements persist, or rather differences show up (10 to 20 undertake). (Received September 20, 2016)