

1116-05-1563

Jonathan Tidor* (jtidor@mit.edu). *Dense binary $PG(t-1, 2)$ -free matroids have critical number $t-1$ or t .*

The critical threshold of a (simple binary) matroid N is the infimum over all ρ such that any N -free matroid M with $|M| > \rho 2^{r(M)}$ has bounded critical number. In this talk, we study the critical threshold of the projective geometry $PG(t-1, 2)$ as a generalization of a classical problem in graph theory. No knowledge of matroid theory will be assumed.

We resolve two conjectures of Geelen and Nelson, showing that the critical threshold of $PG(t-1, 2)$ is $1 - 3 \cdot 2^{-t}$. We do so by proving the following statement: if M is $PG(t-1, 2)$ -free with $|M| > (1 - 3 \cdot 2^{-t}) 2^{r(M)}$, then the critical number of M is $t-1$ or t . (Received September 20, 2015)