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J. Laison, Y. Li, J. Schreiner-McGraw and C. Starr* (cstarr@willamette.edu),
Willamette University, 900 State St, Salem, OR 97301. *Prime Power Graphs and Prime Product Graphs*. Preliminary report.

Let $L : V(G) \rightarrow \mathbb{Z}$ be a one-to-one integer labeling of the vertices of a simple graph G .

(1) We call L a **prime distance labeling** of G if for any two adjacent vertices u and v , the integer $|L(u) - L(v)|$ is prime; in this case, we say G is a **prime distance graph**.

(2) We call L a **k -prime product distance labeling** of G if for any two adjacent vertices u, v , the integer $|L(u) - L(v)|$ is a product of at most k (not necessarily distinct) primes; in this case, we say G is a **k -prime power distance graph**. If G has a k -prime product distance labeling and not a $(k - 1)$ -prime product distance labeling, then we set $\pi(G) = k$.

(3) We call L a **prime power distance labeling** of G if for any two adjacent vertices u and v , the integer $|L(u) - L(v)|$ is a positive power of a prime; in this case, we say G is a **prime power distance graph**.

In this paper, we characterize some families of prime distance graphs, prime power distance graphs, and k -prime product distance graphs; provide bounds for $\pi(G)$; and make connections between graphs of these kinds and several important theorems and conjectures from Number Theory (including the Green-Tao Theorem and Fermat's Last Theorem). (Received September 09, 2015)