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**Sam Mendelson\*** (smendels@gmu.edu) and **Geir Agnarsson**. *Matrix Algebras: Equivalent Ring Relations and Special Presentations*.

A classic result in noncommutative ring theory states that a ring  $R$  is an  $n \times n$  matrix ring if, and only if,  $R$  contains  $n^2$  matrix units  $\{e_{ij}\}_{1 \leq i, j \leq n}$ . In this case  $R \cong M_n(S)$  where  $S$  is a subring of  $R$  that can be described completely in terms of the matrix units. A lesser known result states that a ring  $R$  is an  $(m+n) \times (m+n)$  matrix ring ( $R \cong M_{m+n}(S)$  for some ring  $S$ ) if and only if,  $R$  contains three elements  $a$ ,  $b$ , and  $f$  satisfying the two relations  $af^m + f^nb = 1$  and  $f^{m+n} = 0$ . In this talk, we investigate algebras over a commutative ring (or field) with elements  $c$  and  $f$  satisfying the two relations  $c^i f^m + f^n c^j = 1$  and  $f^{m+n} = 0$ , where  $m = n = 1$ . We will discuss the structure of the underlying ring  $S$  for a general commutative ring  $A$  and investigate these algebras over the fields  $\mathbb{Q}$  and  $\mathbb{F}_p$ , where  $p$  is prime. (Received September 22, 2015)