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**R. Michael Range\*** (range@albany.edu). *A pointwise a-priori estimate for the  $\bar{\partial}$ -Neumann problem on weakly pseudoconvex domains.*

We discuss *pointwise* a-priori estimates for the  $\bar{\partial}$ -Neumann problem on an *arbitrary* weakly pseudoconvex domain  $D$  in  $\mathbb{C}^n$ . Such estimates provide an analogon of the classical basic estimate in the  $L^2$  theory that has been the starting point for all major work in this area involving  $L^2$  and Sobolev norm estimates for the complex Neumann and related operators. In particular, it is shown that for  $(0, q)$  forms  $f$  in the domain of the adjoint  $\bar{\partial}^*$  of  $\bar{\partial}$ , for any coefficient  $f_J$  of  $f$  the pointwise growth of  $\bar{\partial}f_J$  is controlled by the sum of the suprema of  $f$ ,  $\bar{\partial}f$ , and  $\bar{\partial}^*f$  over  $D$  multiplied with  $\text{dist}(z, bD)^{-1+\delta}$ , for any  $\delta < 1/2$ . These results generalize known estimates from the *strictly* pseudoconvex case to general weakly pseudoconvex domains. The proofs utilize the new non-holomorphic Cauchy-Fantappi  kernels recently introduced by the author (Math. Ann. **356** (2013), 793–808) that reflect the complex geometry of the boundary of  $D$ . (Received September 10, 2015)